

47 pts

12-13 CP Pre-Calculus Chapter 1 Test B3

NAME ANSWER KEY

Part 1: Multiple Choice—Write the letter of the correct answer on blank provided.

MC 1 pt each

1. B

1. Jill decides to make cheesecakes to sell at the Fall Festival. Jill spent \$32.00 for the booth decorations and each cheesecake will cost \$6.75 per cake to make. Write a linear function for the total cost of the cheesecakes.

- A) $C(x) = 32x + 6.75$ B) $C(x) = 6.75x + 32$
 C) $C(x) = 38.75x$ D) $C(x) = 26.25x$

2. Given $A = \{(-2, -1, 0)\}$ and $B = \{1, 2, 3\}$, determine which of the sets ordered pairs represents a function from A to B.

- A) $\{(-1, 1), (0, 2), (1, 2), (2, 3)\}$ B) $\{(-1, 2), (0, 1), (-2, 3)\}$
 C) $\{(-1, 2), (0, 2), (1, 3), (2, 3)\}$ D) None of these

3. In which of the following equations is y a function of x ?

- A) $2x - 9 = 17 - 3y$ B) $2x + 5 = |4y|$
 C) Both a and b D) Neither a nor b

4. Given $g(x) = \frac{\sqrt{x-2}}{x-3}$, state the domain of the function.

- A) $[2, \infty)$ B) $[2, 3) \cup (3, \infty)$
 C) $[2, 3]$ D) $(-\infty, 3) \cup (3, \infty)$

5. Given $g(x) = -x^2 + 2x + 1$, find $g(x+4)$

- A) $-x^2 + 10x + 25$ B) $-x^2 - 6x - 7$
 C) $(x+4)^2 + 1$ D) $-x^2 + 2x - 6$

2. B3. A4. B5. B

6. The parent function $f(x) = x^3$ is reflected over the x-axis, has a horizontal shrink of 2 and is translated 3 units up, 4 units to the left. Write the equation of the resulting function.

A) $g(x) = -\left(\frac{1}{2}x - 4\right)^3 + 3$

B) $g(x) = -(2x + 8)^3 + 3$

C) $g(x) = \left(-\frac{1}{2}x - 8\right)^3 + 3$

D) $g(x) = (-2x + 4)^3 + 3$

6. B

7. Determine if $f(x) = -2x^3 - 2x$ is even, odd, or neither.

A) even

B) odd

C) neither

7. B

8. Given the point $(-2, -3)$ on the graph of an even function.

Find a second point on the graph.

A) $(2, -3)$

B) $(-2, 3)$

C) $(2, 3)$

8. A

9. Given $f(x) = \begin{cases} 5 & x \leq -3 \\ -2x+1 & -2 < x \leq 5 \\ 3x^2 & x > 5 \end{cases}$, find $f(5)$. Evaluate the function.

A) 5

B) 75

C) -9

D) 66

9. C

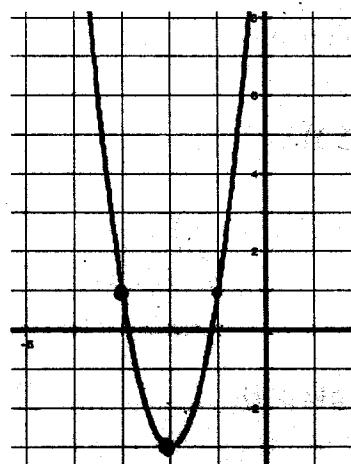
10. What is the equation for the graph at the right?

A) $f(x) = \left(\frac{1}{2}x + 4\right)^2 - 3$

B) $f(x) = (2x + 4)^2 - 3$

C) $f(x) = (2x - 4)^2 - 3$

D) $f(x) = (x - 4)^2 - 3$



10. B

11. Let $f(x) = x + 3$ and $g(x) = x^2 - 4$, find $(fg)(2)$

A) 5

B) 3

C) 0

D) 21

11. C

12. Let $f(x) = x+3$ and $g(x) = x^2 - 4$, find $\left(\frac{f}{g}\right)(x)$ and state the domain.

12. B

A) $\left(\frac{f}{g}\right)(x) = \frac{x}{x^2 - 4}$

domain: $(-\infty, 2)$

C) $\left(\frac{f}{g}\right)(x) = \frac{x+3}{x^2 - 4}$

domain: $(-\infty, -2] \cup [-2, 2] \cup [2, \infty)$

B) $\left(\frac{f}{g}\right)(x) = \frac{x+3}{x^2 - 4}$

domain: $(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$

D) $\left(\frac{f}{g}\right)(x) = \frac{x+3}{x^2 - 4}$

domain: $(-\infty, -3) \cup (3, \infty)$

13. Given $f(x) = 1 - \sqrt{3x+1}$ and $g(x) = 25x^2$, find $(f \circ g)(1)$

13. C

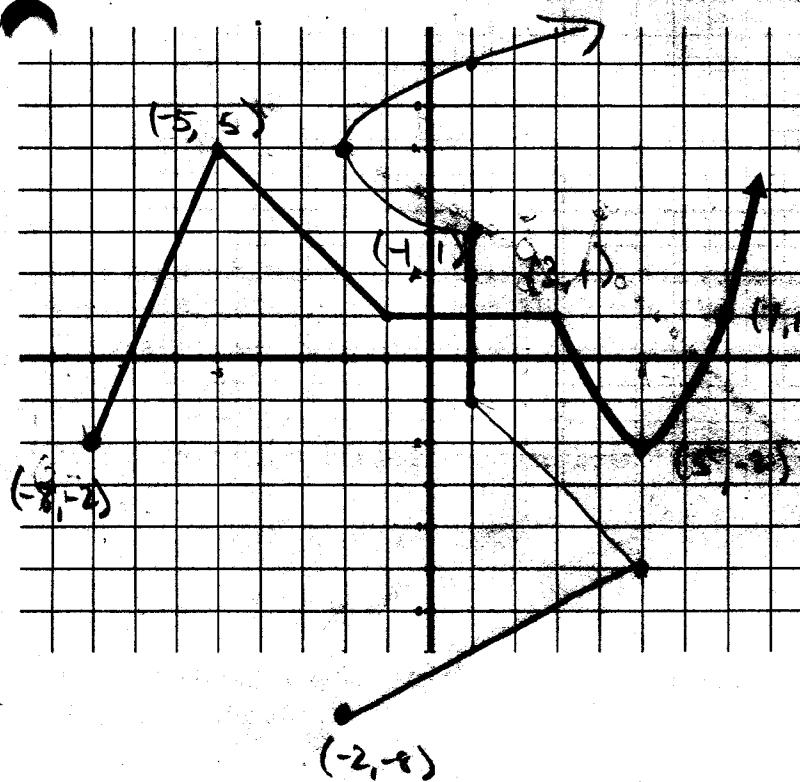
A) -25

B) 25

C) $1 - \sqrt{76}$

D) Not possible

14. Use the graph below to answer the following questions. Use interval notation to answer. 6 pts



A. Function? YES +1/2

B. Domain: $[-8, \infty)$ +1/2

C. Range: $[1, \infty)$ +1/2

D. Interval(s) of Increase: $[-8, -5] \cup (5, \infty)$ +1/2

E. Interval(s) of Decrease: $(-5, -1) \cup (3, 5)$ +1/2

F. Is the inverse a function? NO +1/2

G. Even, Odd, neither? Neither +1/2

H. Find $f(4)$: 9 -1

I. What is x if $f(x) = 1$: $[-1, 3]$ +1/2

I. Graph the inverse of the function
(Use the same coordinate plane) +1/2

+18

15. Given $f(x) = \sqrt[3]{x-2} + 1$

A. What is the domain of f ?

$$x \geq 2$$

C. Find the inverse of f .

$$x = \sqrt[3]{y-2} + 1$$

$$x - 1 = \sqrt[3]{y-2}$$

$$(x-1)^3 = y-2$$

$$y = (x-1)^3 + 2$$

16. Use the composition of functions to prove $f(x) = \sqrt[3]{3x-10}$ and $g(x) = \frac{x^3+10}{3}$ are inverses.

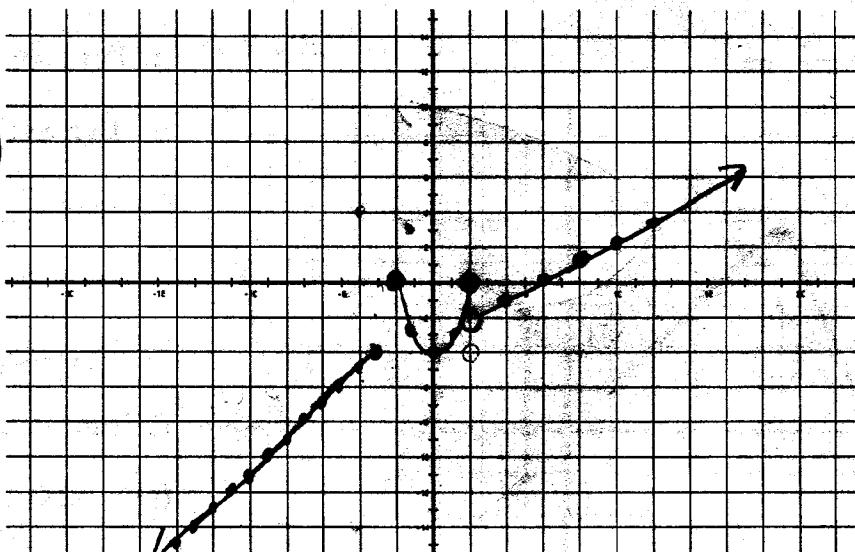
$$\begin{aligned} f(g(x)) &= \sqrt[3]{3\left(\frac{x^3+10}{3}\right) - 10} \\ &= \sqrt[3]{x^3 + 10 - 10} \\ &= \sqrt[3]{x^3} \\ &= x \end{aligned}$$

$$g(f(x)) = \frac{(\sqrt[3]{3x-10})^3 + 10}{3} = \frac{3x-10 + 10}{3} = \frac{3x}{3} = x$$

17. Graph the piecewise function.

$$f(x) = \begin{cases} -|x-1| & x < -3 \\ x^2 - 4 & -2 \leq x \leq 2 \\ \frac{x-3}{2} & x > 2 \end{cases}$$

x	$- x-1 $	$x^2 - 4$	$\frac{x-3}{2}$
-3	-4	-3	-3
-2	0	0	-2
-1	0	-3	-1
0	1	-4	0
1	0	-3	1
2	-4	0	2



+5 15. A. $(-\infty, \infty) \cup \{1\}$

B. $(-\infty, \infty) \cup \{1\}$

+3 C. $f^{-1}(x) = (x-1)^3 + 2$

Domain: $(-\infty, \infty)$

Range: $(-\infty, \infty)$

8. Use transformations to graph the function.

$$f(x) = 1 - 3\sqrt{2 + \frac{1}{2}x}$$

$$f(x) = -3\sqrt{\frac{1}{2}(x+4)} + 1 \quad (+1)$$

A. Graph the parent function using a dotted curve.
(Use the coordinate plane provided.)

B. List the transformations in the correct order

C. Write the list of order pairs for the final graph.

D. Graph $f(x)$.

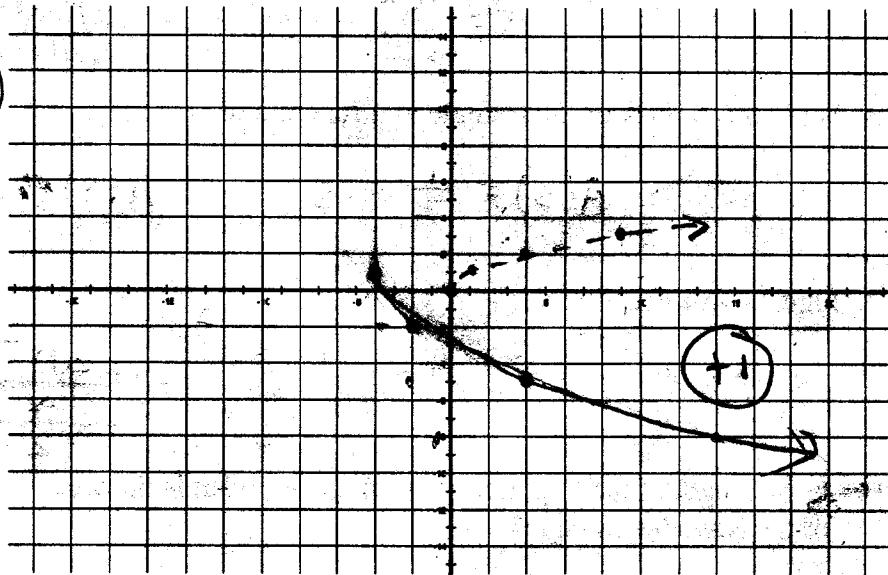
(On the same coordinate plane as part A)

$$P(x) = \sqrt{x}$$

x	P(x)	R	S
0	0	0	0
1	1	P	-P
4	2	4	-2
9	3	9	-3

$$\frac{1}{2}(x+4)$$

$$+3$$



19. Christina is making hot chocolate to sell at this season's first football game.

She spent \$25.00 on paper supplies. Each cup of hot chocolate costs Christina 75 cents to make. She plans on selling each cup of hot chocolate for \$2.50.

15. A. \$2.50.00 (+1)

$$P(x) = .75x + 25 \quad (+1)$$

A. Write a cost function and determine the cost for making 300 cups of hot chocolate.

$$C(x) = .75x + 25.00$$

$$C(300) = .75(300) + 25.00$$

$$\frac{3}{4}(300)$$

$$225 + 25.00$$

$$R(x) = 2.5x$$

B. Write a profit function and then determine how many cups must be sold to make \$325

$$P(x) = 2.5x - (.75x + 25)$$

$$P(x) = 1.75x - 25$$

$$\begin{array}{r} 2.50 \\ - .75 \\ \hline 1.75 \end{array}$$

$$B. P(x) = 1.75x - 25 \quad (+1)$$

$$200$$

(+1)

$$\frac{7}{4}x = 350$$

$$x = 350 \cdot \frac{4}{7}$$

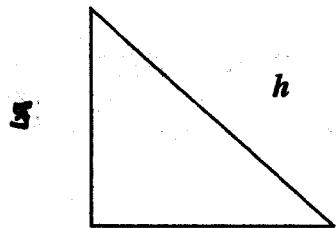
$$x = 50 \cdot 4 = 200 \quad (+10)$$

$$325 = 1.75x - 25$$

$$350 = 1.75x$$

$$350 = 1.75x$$

20. Given an isosceles right triangle.



15
20. A. $S(h) = \frac{h\sqrt{2}}{2}$

B. $A(s) = \frac{s^2}{2}$

C. $\frac{h^2}{4}$

D. 25

A. Write the length of the side S , as a function of the length of the hypotenuse h .

$$2S^2 = h^2$$

$$S = \sqrt{\frac{h^2}{2}} \quad S(h) = \frac{h}{\sqrt{2}} = \frac{h\sqrt{2}}{2}$$

B. Write the Area A of the triangle as a function of side S .

$$A(s) = \frac{1}{2} s \cdot s = A(s) = \frac{s^2}{2}$$

C. Find $(A \circ S)(h)$.

$$A(S(h)) = A = \frac{\left(\frac{h\sqrt{2}}{2}\right)^2}{2} = \frac{\frac{2h^2}{4}}{2} = \frac{h^2}{2} = \frac{h^2}{4}$$

D. If the length of the hypotenuse is 10 inches, what is the area of the isosceles triangle?

$$A = \frac{10^2}{4} = \frac{100}{4} = 25$$

15